

King Abdul Aziz University	Faculty of Sciences	Mathematics Department
Math 110	Final Test Fall 2013 (40 Marks)	Time 120 m
Student Name:	Student Number: <input type="text" value="A"/>	

1) If  $f(x) = 2x - 9$ , then  $f^{-1}(x) =$

- [a]  $\frac{x-9}{2}$      [b]  $\frac{x}{2} - 9$      [c]  $\frac{x+9}{2}$      [d]  $\frac{x}{2} + 9$

2) If  $y = \sqrt{3x^2 + 6x}$ , then  $y' =$

- [a]  $\frac{6(x+1)}{\sqrt{3x^2 + 6x}}$      [b]  $\frac{x+6}{\sqrt{3x^2 + 6x}}$      [c]  $\frac{3(x+1)}{\sqrt{3x^2 + 6x}}$      [d]  $\frac{x+1}{2\sqrt{3x^2 + 6x}}$

3) If  $y = \log_5(x^3 - 2\csc x)$ , then  $y' =$

- [a]  $\frac{3x^2 + 2\csc x \cot x}{x^3 - 2\csc x}$      [b]  $\frac{3x^2 + 2\csc x \cot x}{x^3 - 2\csc x \ln 5}$   
 [c]  $\frac{3x^2 + 2\csc x \cot x}{(x^3 - 2\csc x) \ln 5}$      [d]  $\frac{3x^2 - 2\csc x \cot x}{(x^3 - 2\csc x) \ln 5}$

4) If  $-7 \leq 2x + 3 < 5$ , then  $x =$

- [a]  $(-5, 1)$      [b]  $(-5, 1]$      [c]  $[-5, 1)$      [d]  $[-5, 1]$

5) If  $f(x) = x^2$ , then  $f'(x) =$

- [a]  $\lim_{x \rightarrow 0} \frac{(x+h)^2 - x^2}{h}$      [b]  $\lim_{x \rightarrow 0} \frac{(x+h)^2 + x^2}{h}$   
 [c]  $\lim_{h \rightarrow 0} \frac{(x+h)^2 + x^2}{h}$      [d]  $\lim_{h \rightarrow 0} \frac{(x+h)^2 - x^2}{h}$

6) The function  $f(x) = \frac{x+1}{x^2 - 4}$  is continuous on

- [a]  $\{\pm 2\}$      [b]  $[-2, 2]$      [c]  $\{x \in \mathbb{R} : x \neq \pm 2\}$      [d]  $(-\infty, -2) \cup (2, \infty)$

7) The domain of  $\frac{x+3}{\sqrt{x^2 - 4}}$  is

- [a]  $[-2, 2]$      [b]  $(-2, 2)$      [c]  $(-\infty, -2) \cup (2, \infty)$      [d]  $(-\infty, -2] \cup [2, \infty)$

8)  $\csc(\tan^{-1} x) =$

- [A]  $\frac{1}{\sqrt{x^2 + 1}}$      [B]  $\frac{x}{\sqrt{x^2 + 1}}$      [C]  $\sqrt{x^2 + 1}$      [D]  $\frac{\sqrt{x^2 + 1}}{x}$

9)  $\lim_{x \rightarrow 5^+} \frac{x+1}{x-5} =$

- [a] -5       [b] 5       [c]  $-\infty$        [d]  $\infty$

10)  $\lim_{x \rightarrow 1} \frac{x^2-1}{x-1} =$

- [a] 0       [b] does not exist       [c] 2       [d]  $\frac{1}{2}$

11) The values in  $(-1, 3)$  which makes  $f(x) = x^2 - 5x + 7$  satisfied Mean Value Theorem on  $[-1, 3]$  is

- [a] 1       [b] -4       [c] 0       [d] 2

12)  $\lim_{x \rightarrow \infty} \left( \sqrt{x^2+x} - x \right) =$

- [a] 1       [b]  $-\frac{1}{2}$        [c] 0       [d]  $\frac{1}{2}$

13) If  $y = \ln(\cos x)$ , then  $y' =$

- [a]  $\tan x$        [b]  $-\tan x$        [c]  $\cot x$        [d]  $-\cot x$

14) If  $f(x) = \tan^{-1}(x)$  and  $g(x) = \tan(x)$  then  $(f \circ g)(x) =$

- [a]  $\tan^{-1} x \tan x$        [b]  $x$        [c] 1       [d]  $\tan x$

15) The absolute maximum value of  $f(x) = x^3 - 6x^2 + 9x + 2$  on  $[0, 4]$  is

- [a] 2       [b] 6       [c] 7       [d] 12

16) The absolute minimum value of  $f(x) = x^3 - 6x^2 + 9x + 2$  on  $[0, 4]$  is

- [a] 2       [b] 6       [c] 0       [d] -3

17) If  $y = x^x$ , then  $y' =$

- [a]  $x^x(1+\ln x)$        [b]  $1+\ln x$        [c]  $x^x$        [d]  $x^x \ln x$

18) If  $y = \tan^{-1}\left(\frac{2x}{3}\right)$ , then  $y' =$

- [a]  $-\frac{6}{9+4x^2}$        [b]  $\frac{9}{9+4x^2}$        [c]  $-\frac{9}{9+4x^2}$        [d]  $\frac{6}{9+4x^2}$

19) If  $x^2 + y^2 = 3xy + 7$ , then  $y' =$

- [a]  $\frac{2x+y}{3x-2y}$        [b]  $\frac{3y-2x}{2y-3x}$        [c]  $\frac{2x}{3-2y}$        [d]  $\frac{2x}{y}$

20) If  $y = \sin x \sec x$ , then  $y' =$

- a)  $\sin x \tan x + 1$      b)  $\sec^2 x$      c)  $\sin x \tan x - 1$      d)  $\sin x \sec x \tan x - 1$

21) If  $y = \sin^3(4x)$ , then  $y' =$

- a)  $4\cos^3(4x)$      b)  $3\sin^2(4x)\cos(4x)$   
 c)  $12\sin^2(4x)\cos(4x)$      d)  $4\sin^3(4x) + 12\sin^2 x \cos x$

22) The tangent line equation to the curve  $y = \frac{2x}{x+1}$  at the point  $(0,0)$  is

- a)  $y = -2x$      b)  $y = -2x + 1$      c)  $y = 2x$      d)  $y = 2x - 1$

23) If  $y = 3^x \cot x$ , then  $y' =$

- a)  $3^x \ln 3 \cot x + 3^x \sec^2 x$      b)  $3^x \cot x + 3^x \sec^2 x$   
 c)  $3^x \cot x - 3^x \csc^2 x$      d)  $3^x \ln 3 \cot x - 3^x \csc^2 x$

24) If  $y = (2x^2 + \sec x)^7$ , then  $y' =$

- a)  $7(2x^2 + \sec x)^6$      b)  $7(2x^2 + \sec x)^6(4x - \sec x \tan x)$   
 c)  $7(2x^2 + \sec x)^6(4x + \sec x \tan x)$      d)  $28x(2x^2 + \sec x)^6$

25) The slope of the perpendicular line to the line  $3y - 2x - 6 = 0$  is

- a)  $\frac{2}{3}$      b)  $-\frac{2}{3}$      c)  $-\frac{3}{2}$      d)  $\frac{3}{2}$

26) If the graph of the function  $f(x) = 3^x$  is shifted a distance 2 units upward, then the new graph represented the graph of the function

- a)  $3^{x+2}$      b)  $3^x + 2$      c)  $3^{x-2}$      d)  $3^x - 2$

27) If  $y = \ln \frac{x+1}{x-2}$ , then  $y' =$

- a)  $-\frac{3}{(x+1)(x-2)}$      b)  $\frac{3}{(x+1)(x-2)}$   
 c)  $\frac{1}{(x+1)(x-2)}$      d)  $-\frac{1}{(x+1)(x-2)}$

28)  $\lim_{x \rightarrow 0} \frac{\sin 3x}{5x} =$

- a)  $\frac{3}{5}$      b)  $\frac{5}{3}$      c)  $\frac{1}{5}$      d) 3

29) $D^{(125)}(\cos x) =$	<input type="checkbox"/> a) $\sin x$	<input type="checkbox"/> b) $-\sin x$	<input type="checkbox"/> c) $\cos x$	<input type="checkbox"/> d) $-\cos x$
30) $\frac{5\pi}{6}$ rad =	<input type="checkbox"/> a) $120^\circ$	<input type="checkbox"/> b) $150^\circ$	<input type="checkbox"/> c) $270^\circ$	<input type="checkbox"/> d) $210^\circ$
31) The distance between the points $(-1, 2)$ and $(2, -1)$ is	<input type="checkbox"/> a) $2\sqrt{3}$	<input type="checkbox"/> b) $3\sqrt{2}$	<input type="checkbox"/> c) 9	<input type="checkbox"/> d) 3
32) If $y = e^{2x}$ , then $y^{(5)} =$	<input type="checkbox"/> a) $128e^{2x}$	<input type="checkbox"/> b) $16e^{2x}$	<input type="checkbox"/> c) $64e^{2x}$	<input type="checkbox"/> d) $32e^{2x}$
33) The critical numbers of the function $f(x) = 2x^3 + 3x^2 - 12x + 15$ are	<input type="checkbox"/> a) $1, -2$	<input type="checkbox"/> b) $-1, 2$	<input type="checkbox"/> c) $1, 2$	<input type="checkbox"/> d) $-1, -2$
34) The function $f(x) = 2x^3 + 3x^2 - 12x + 15$ is increasing on	<input type="checkbox"/> a) $(-\infty, -2) \cup (-1, \infty)$	<input type="checkbox"/> b) $(-\infty, -2) \cup (1, \infty)$	<input type="checkbox"/> c) $(-\infty, -1) \cup (2, \infty)$	<input type="checkbox"/> d) $(-\infty, 1) \cup (2, \infty)$
35) The function $f(x) = 2x^3 + 3x^2 - 12x + 15$ is decreasing on	<input type="checkbox"/> a) $(-2, -1)$	<input type="checkbox"/> b) $(-2, 1)$	<input type="checkbox"/> c) $(1, 2)$	<input type="checkbox"/> d) $(-1, 2)$
36) The function $f(x) = 2x^3 + 3x^2 - 12x + 15$ has a relative maximum at	<input type="checkbox"/> a) $(1, 8)$	<input type="checkbox"/> b) $(-1, 28)$	<input type="checkbox"/> c) $(2, 19)$	<input type="checkbox"/> d) $(-2, 35)$
37) The function $f(x) = 2x^3 + 3x^2 - 12x + 15$ has a relative minimum at	<input type="checkbox"/> a) $(1, 8)$	<input type="checkbox"/> b) $(-1, 28)$	<input type="checkbox"/> c) $(2, 19)$	<input type="checkbox"/> d) $(-2, 35)$
38) The graph of $f(x) = 2x^3 + 3x^2 - 12x + 15$ is concave upward on	<input type="checkbox"/> a) $(-\infty, \frac{1}{2})$	<input type="checkbox"/> b) $(-\infty, -\frac{1}{2})$	<input type="checkbox"/> c) $(-\frac{1}{2}, \infty)$	<input type="checkbox"/> d) $(\frac{1}{2}, \infty)$
39) The graph of $f(x) = 2x^3 + 3x^2 - 12x + 15$ is concave downward on	<input type="checkbox"/> a) $(-\infty, \frac{1}{2})$	<input type="checkbox"/> b) $(-\infty, -\frac{1}{2})$	<input type="checkbox"/> c) $(-\frac{1}{2}, \infty)$	<input type="checkbox"/> d) $(\frac{1}{2}, \infty)$
40) The function $f(x) = 2x^3 + 3x^2 - 12x + 15$ has an inflection at	<input type="checkbox"/> a) $(\frac{1}{2}, 10)$	<input type="checkbox"/> b) $(-\frac{1}{2}, 10)$	<input type="checkbox"/> c) $(\frac{1}{2}, \frac{43}{2})$	<input type="checkbox"/> d) $(-\frac{1}{2}, \frac{43}{2})$

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1) If  $y = \cos x \csc x$ , then  $y' =$

- a)  $-\csc^2 x$      b)  $1 - \cos x \cot x$      c)  $-1 + \cos x \cot x$      d)  $1 - \cos x \csc x \cot x$

2) If  $f(x) = \cot^{-1}(x)$  and  $g(x) = \cot(x)$  then  $(f \circ g)(x) =$

- a) 1     b)  $\cot x \cot^{-1} x$      c)  $x$      d)  $\cot x$

3) The function  $f(x) = \frac{x+1}{x^2-49}$  is continuous on

- a)  $\{x \in \mathbb{R} : x \neq \pm 7\}$      b)  $[-7, 7]$      c)  $(-\infty, -7) \cup (7, \infty)$      d)  $\{\pm 7\}$

4) If  $x^2 - 4 = 3xy - y^2$ , then  $y' =$

- a)  $\frac{3y - 2x}{2y - 3x}$      b)  $\frac{2x}{y}$      c)  $\frac{2x}{3 - 2y}$      d)  $\frac{2x + y}{3x - 2y}$

5) If  $y = 3^x \tan x$ , then  $y' =$

- a)  $3^x \ln 3 \tan x - 3^x \sec^2 x$      b)  $3^x \ln 3 \tan x + 3^x \sec^2 x$   
 c)  $3^x \tan x - 3^x \sec^2 x$      d)  $3^x \tan x + 3^x \sec^2 x$

6) If  $y = \log_5(x^3 - 2 \csc x)$ , then  $y' =$

- a)  $\frac{3x^2 + 2 \csc x \cot x}{(x^3 - 2 \csc x) \ln 5}$      b)  $\frac{3x^2 + 2 \csc x \cot x}{x^3 - 2 \csc x \ln 5}$   
 c)  $\frac{3x^2 + 2 \csc x \cot x}{x^3 - 2 \csc x}$      d)  $\frac{3x^2 - 2 \csc x \cot x}{(x^3 - 2 \csc x) \ln 5}$

7) If  $y = (2x^2 + \csc x)^7$ , then  $y' =$

- a)  $7(2x^2 + \csc x)^6 (4x - \csc x \cot x)$      b)  $7(2x^2 + \csc x)^6$   
 c)  $7(2x^2 + \csc x)^6 (4x + \csc x \cot x)$      d)  $28x(2x^2 + \csc x)^6$

8) The absolute minimum value of  $f(x) = x^3 - 6x^2 + 9x + 2$  on  $[0, 4]$  is

- a) 6     b) 0     c) 2     d) -3

9) The absolute maximum value of  $f(x) = x^3 - 6x^2 + 9x + 2$  on  $[0, 4]$  is

- a) 6     b) 2     c) 7     d) 12

10) If  $y = \sqrt{3x^2 - 6x}$ , then  $y' =$

- [a]  $\frac{x-6}{\sqrt{3x^2-6x}}$    [b]  $\frac{6(x-1)}{\sqrt{3x^2-6x}}$    [c]  $\frac{x-1}{2\sqrt{3x^2-6x}}$    [d]  $\frac{3(x-1)}{\sqrt{3x^2-6x}}$

11) The slope of the perpendicular line to the line  $2y + 3x - 6 = 0$  is

- [a]  $\frac{2}{3}$    [b]  $-\frac{2}{3}$    [c]  $-\frac{3}{2}$    [d]  $\frac{3}{2}$

12) If  $y = \ln \frac{x+1}{x-2}$ , then  $y' =$

- [a]  $\frac{3}{(x+1)(x-2)}$    [b]  $-\frac{3}{(x+1)(x-2)}$   
[c]  $\frac{1}{(x+1)(x-2)}$    [d]  $-\frac{1}{(x+1)(x-2)}$

13)  $\sec(\tan^{-1} x) =$

- [A]  $\frac{1}{\sqrt{x^2+1}}$    [B]  $\frac{x}{\sqrt{x^2+1}}$    [C]  $\sqrt{x^2+1}$    [D]  $\frac{\sqrt{x^2+1}}{x}$

14)  $\lim_{x \rightarrow 0} \frac{\tan 5x}{3x} =$

- [a]  $\frac{1}{3}$    [b] 5   [c]  $\frac{3}{5}$    [d]  $\frac{5}{3}$

15) If  $f(x) = 2x + 7$ , then  $f^{-1}(x) =$

- [a]  $\frac{x+7}{2}$    [b]  $\frac{x}{2}-7$    [c]  $\frac{x}{2}+7$    [d]  $\frac{x-7}{2}$

16)  $D^{(127)}(\cos x) =$

- [a]  $\sin x$    [b]  $-\sin x$    [c]  $\cos x$    [d]  $-\cos x$

17)  $\lim_{x \rightarrow \infty} \left( \sqrt{x^2+x} - x \right) =$

- [a]  $\frac{1}{2}$    [b] 1   [c] 0   [d]  $-\frac{1}{2}$

18) If  $y = \sin^4(3x)$ , then  $y' =$

- [a]  $12\sin^3(3x)\cos(3x)$    [b]  $4\sin^3(3x)\cos(3x)$   
[c]  $3\cos^2(3x)$    [d]  $3\sin^4(3x) + 12\sin^3 x \cos x$

19)  $\frac{2\pi}{3}$  rad =

[a]  $120^\circ$

[b]  $150^\circ$

[c]  $270^\circ$

[d]  $210^\circ$

20) If  $f(x) = x^2$ , then  $f'(x) =$

[a]  $\lim_{h \rightarrow 0} \frac{(x+h)^2 - x^2}{h}$

[b]  $\lim_{x \rightarrow 0} \frac{(x+h)^2 + x^2}{h}$

[c]  $\lim_{h \rightarrow 0} \frac{(x+h)^2 + x^2}{h}$

[d]  $\lim_{x \rightarrow 0} \frac{(x+h)^2 - x^2}{h}$

21) The tangent line equation to the curve  $y = \frac{2x}{x-1}$  at the point  $(0,0)$  is

[a]  $y = -2x - 1$

[b]  $y = 2x + 1$

[c]  $y = 2x$

[d]  $y = -2x$

22) If the graph of the function  $f(x) = 3^x$  is shifted a distance 2 units to the right, then the new graph represented the graph of the function

[a]  $3^{x+2}$

[b]  $3^x + 2$

[c]  $3^{x-2}$

[d]  $3^x - 2$

23) The distance between the points  $(-1, 2)$  and  $(2, -1)$  is

[a] 3

[b]  $2\sqrt{3}$

[c] 9

[d]  $3\sqrt{2}$

24) If  $y = \ln(\sin x)$ , then  $y' =$

[a]  $\tan x$

[b]  $-\tan x$

[c]  $\cot x$

[d]  $-\cot x$

25) If  $-7 \leq 2x + 3 \leq 5$ , then  $x =$

[a]  $(-5, 1)$

[b]  $(-5, 1]$

[c]  $[-5, 1)$

[d]  $[-5, 1]$

26) If  $y = \cot^{-1}\left(\frac{2x}{3}\right)$ , then  $y' =$

[a]  $-\frac{6}{9+4x^2}$

[b]  $\frac{9}{9+4x^2}$

[c]  $-\frac{9}{9+4x^2}$

[d]  $\frac{6}{9+4x^2}$

27) If  $y = e^{2x}$ , then  $y^{(4)} =$

[a]  $128e^{2x}$

[b]  $16e^{2x}$

[c]  $64e^{2x}$

[d]  $32e^{2x}$

28)  $\lim_{x \rightarrow 3^-} \frac{x+1}{x-3} =$

[a] 3

[b]  $\infty$

[c] -3

[d]  $-\infty$

29) If  $y = x^x$ , then  $y' =$

[a]  $1 + \ln x$

[b]  $x^x$

[c]  $x^x(1 + \ln x)$

[d]  $x^x \ln x$

30)	The critical numbers of the function $f(x) = 2x^3 - 3x^2 - 12x + 15$ are						
<input type="checkbox"/> a	1, -2	<input type="checkbox"/> b	-1, 2	<input type="checkbox"/> c	1, 2	<input type="checkbox"/> d	-1, -2
31)	The function $f(x) = 2x^3 - 3x^2 - 12x + 15$ is increasing on						
<input type="checkbox"/> a	$(-\infty, -2) \cup (-1, \infty)$	<input type="checkbox"/> b	$(-\infty, -2) \cup (1, \infty)$	<input type="checkbox"/> c	$(-\infty, -1) \cup (2, \infty)$	<input type="checkbox"/> d	$(-\infty, 1) \cup (2, \infty)$
32)	The function $f(x) = 2x^3 - 3x^2 - 12x + 15$ is decreasing on						
<input type="checkbox"/> a	$(-2, -1)$	<input type="checkbox"/> b	$(-2, 1)$	<input type="checkbox"/> c	$(1, 2)$	<input type="checkbox"/> d	$(-1, 2)$
33)	The function $f(x) = 2x^3 - 3x^2 - 12x + 15$ has a relative maximum at						
<input type="checkbox"/> a	$(1, 2)$	<input type="checkbox"/> b	$(-1, 22)$	<input type="checkbox"/> c	$(2, -5)$	<input type="checkbox"/> d	$(-2, 11)$
34)	The function $f(x) = 2x^3 - 3x^2 - 12x + 15$ has a relative minimum at						
<input type="checkbox"/> a	$(1, 2)$	<input type="checkbox"/> b	$(-1, 22)$	<input type="checkbox"/> c	$(2, -5)$	<input type="checkbox"/> d	$(-2, 11)$
35)	The graph of $f(x) = 2x^3 - 3x^2 - 12x + 15$ concave upward on						
<input type="checkbox"/> a	$(-\infty, \frac{1}{2})$	<input type="checkbox"/> b	$(-\infty, -\frac{1}{2})$	<input type="checkbox"/> c	$(-\frac{1}{2}, \infty)$	<input type="checkbox"/> d	$(\frac{1}{2}, \infty)$
36)	The graph of $f(x) = 2x^3 - 3x^2 - 12x + 15$ concave downward on						
<input type="checkbox"/> a	$(-\infty, \frac{1}{2})$	<input type="checkbox"/> b	$(-\infty, -\frac{1}{2})$	<input type="checkbox"/> c	$(-\frac{1}{2}, \infty)$	<input type="checkbox"/> d	$(\frac{1}{2}, \infty)$
37)	The function $f(x) = 2x^3 - 3x^2 - 12x + 15$ has an inflection at						
<input type="checkbox"/> a	$(\frac{1}{2}, 20)$	<input type="checkbox"/> b	$(-\frac{1}{2}, 20)$	<input type="checkbox"/> c	$(\frac{1}{2}, \frac{17}{2})$	<input type="checkbox"/> d	$(-\frac{1}{2}, \frac{17}{2})$
38)	$\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1} =$						
<input type="checkbox"/> a	0	<input type="checkbox"/> b	does not exist	<input type="checkbox"/> c	2	<input type="checkbox"/> d	$\frac{1}{2}$
39)	The domain of $\frac{x+3}{\sqrt{4-x^2}}$ is						
<input type="checkbox"/> a	$[-2, 2]$	<input type="checkbox"/> b	$(-\infty, -2) \cup (2, \infty)$	<input type="checkbox"/> c	$(-2, 2)$	<input type="checkbox"/> d	$(-\infty, -2] \cup [2, \infty)$
40)	The values in $(-1, 3)$ which makes $f(x) = x^2 - 5x + 7$ satisfied Mean Value Theorem on $[-1, 3]$ is						
<input type="checkbox"/> a	-4	<input type="checkbox"/> b	0	<input type="checkbox"/> c	1	<input type="checkbox"/> d	2

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1)  $\lim_{x \rightarrow 5^+} \frac{x+1}{x-5} =$

- [a]  $\infty$        [b]  $-\infty$        [c] 5       [d] -5

2)  $\lim_{x \rightarrow \infty} \left( \sqrt{x^2 + x} - x \right) =$

- [a] 1       [b]  $\frac{1}{2}$        [c] 0       [d]  $-\frac{1}{2}$

3)  $y = -\ln(\cos x)$ , then  $y' =$

- [a]  $\tan x$        [b]  $-\tan x$        [c]  $\cot x$        [d]  $-\cot x$

4) The absolute maximum value of  $f(x) = x^3 - 6x^2 + 9x + 2$  on  $[0, 4]$  is

- [a] 2       [b] 12       [c] 7       [d] 6

5) The absolute minimum value of  $f(x) = x^3 - 6x^2 + 9x + 2$  on  $[0, 4]$  is

- [a] 6       [b] 2       [c] 0       [d] -3

6) If  $f(x) = \tan^{-1}(x)$  and  $g(x) = \tan(x)$  then  $(f \circ g)(x) =$

- [a]  $x$        [b]  $\tan^{-1} x \tan x$        [c] 1       [d]  $\tan x$

7) If  $y = x^x$ , then  $y' =$

- [a]  $1 + \ln x$        [b]  $x^x(1 + \ln x)$        [c]  $x^x$        [d]  $x^x \ln x$

8) If  $x^2 + y^2 - 5 = 3xy$ , then  $y' =$

- [a]  $\frac{2x+y}{3x-2y}$        [b]  $\frac{2x}{y}$        [c]  $\frac{2x}{3-2y}$        [d]  $\frac{3y-2x}{2y-3x}$

9) The tangent line equation to the curve  $y = \frac{2x}{x+1}$  at the point  $(0,0)$  is

- [a]  $y = 2x$        [b]  $y = -2x + 1$        [c]  $y = -2x$        [d]  $y = 2x - 1$

10) If  $y = 3^x \cot x$ , then  $y' =$

- [a]  $3^x \ln 3 \cot x - 3^x \csc^2 x$        [b]  $3^x \cot x + 3^x \sec^2 x$   
 [c]  $3^x \cot x - 3^x \csc^2 x$        [d]  $3^x \ln 3 \cot x + 3^x \sec^2 x$

11)  $D^{(126)}(\cos x) =$

- [a]  $\sin x$        [b]  $-\sin x$        [c]  $\cos x$        [d]  $-\cos x$

12) If  $f(x) = 2x - 5$ , then  $f^{-1}(x) =$

- [a]  $\frac{x+5}{2}$  [b]  $\frac{x}{2} - 5$  [c]  $\frac{x-5}{2}$  [d]  $\frac{x}{2} + 5$

13) The slope of the perpendicular line to the line  $3y + 2x - 6 = 0$  is

- [a]  $\frac{2}{3}$  [b]  $-\frac{2}{3}$  [c]  $-\frac{3}{2}$  [d]  $\frac{3}{2}$

14) If the graph of the function  $f(x) = 3^x$  is shifted a distance 2 units downward, then the new graph represented the graph of the function

- [a]  $3^{x+2}$  [b]  $3^x + 2$  [c]  $3^{x-2}$  [d]  $3^x - 2$

15) If  $y = \ln \frac{x+1}{x-2}$ , then  $y' =$

- [a]  $\frac{1}{(x+1)(x-2)}$  [b]  $-\frac{1}{(x+1)(x-2)}$  [c]  $\frac{3}{(x+1)(x-2)}$  [d]  $-\frac{3}{(x+1)(x-2)}$

16)  $\lim_{x \rightarrow 0} \frac{\sin 5x}{3x} =$

- [a]  $\frac{3}{5}$  [b]  $\frac{5}{3}$  [c]  $\frac{1}{3}$  [d] 5

17) If  $y = (2x^2 + \sec x)^7$ , then  $y' =$

- [a]  $7(2x^2 + \sec x)^6(4x + \sec x \tan x)$  [b]  $7(2x^2 + \sec x)^6(4x - \sec x \tan x)$   
[c]  $28x(2x^2 + \sec x)^6$  [d]  $7(2x^2 + \sec x)^6(4x + \sec x \tan x)$

18) If  $f(x) = x^2$ , then  $f'(x) =$

- [a]  $\lim_{x \rightarrow 0} \frac{(x+h)^2 + x^2}{h}$  [b]  $\lim_{h \rightarrow 0} \frac{(x+h)^2 - x^2}{h}$

- [c]  $\lim_{h \rightarrow 0} \frac{(x+h)^2 + x^2}{h}$  [d]  $\lim_{x \rightarrow 0} \frac{(x+h)^2 - x^2}{h}$

19)  $\frac{7\pi}{6}$  rad =

- [a]  $120^\circ$  [b]  $150^\circ$  [c]  $270^\circ$  [d]  $210^\circ$

20) If  $y = \sin x \sec x$ , then  $y' =$

- [a]  $\sin x \tan x + 1$  [b]  $\sin x \sec x \tan x - 1$  [c]  $\sin x \tan x - 1$  [d]  $\sec^2 x$

21) The values in  $(-1,3)$  which makes  $f(x) = x^2 - 5x + 7$  satisfied Mean Value Theorem on  $[-1,3]$  is

- a) -4     b) 1     c) 0     d) 2

22) The function  $f(x) = \frac{x+1}{x^2-9}$  is continuous on

- a)  $\{\pm 3\}$      b)  $[-3,3]$      c)  $(-\infty, -3) \cup (3, \infty)$      d)  $\{x \in \mathbb{R} : x \neq \pm 3\}$

23)  $\cos(\tan^{-1} x) =$

- A)  $\frac{1}{\sqrt{x^2+1}}$      B)  $\frac{x}{\sqrt{x^2+1}}$      C)  $\sqrt{x^2+1}$      D)  $\frac{\sqrt{x^2+1}}{x}$

24) The distance between the points  $(-1,2)$  and  $(2,-1)$  is

- a)  $3\sqrt{2}$      b)  $2\sqrt{3}$      c) 9     d) 3

25) If  $-7 < 2x + 3 \leq 5$ , then  $x =$

- a)  $(-5,1)$      b)  $(-5,1]$      c)  $[-5,1)$      d)  $[-5,1]$

26) If  $y = e^{2x}$ , then  $y^{(6)} =$

- a)  $128e^{2x}$      b)  $16e^{2x}$      c)  $64e^{2x}$      d)  $32e^{2x}$

27) If  $y = \sin^3(4x)$ , then  $y' =$

- a)  $4\cos^3(4x)$      b)  $3\sin^2(4x)\cos(4x)$   
 c)  $4\sin^3(4x) + 12\sin^2 x \cos x$      d)  $12\sin^2(4x)\cos(4x)$

28) The domain of  $\frac{x+3}{\sqrt{x^2-4}}$  is

- a)  $[-2,2]$      b)  $(-\infty, -2) \cup (2, \infty)$      c)  $(-2,2)$      d)  $(-\infty, -2] \cup [2, \infty)$

29)  $\lim_{x \rightarrow 3} \frac{x^2-9}{x-3} =$

- a) -6     b) 6     c)  $\infty$      d) 0

30) If  $y = \sqrt{3x^2 + 6x}$ , then  $y' =$

- a)  $\frac{x+6}{\sqrt{3x^2+6x}}$      b)  $\frac{6(x+1)}{\sqrt{3x^2+6x}}$   
 c)  $\frac{x+1}{2\sqrt{3x^2+6x}}$      d)  $\frac{3(x+1)}{\sqrt{3x^2+6x}}$

31) If  $y = \tan^{-1}\left(\frac{3x}{2}\right)$ , then  $y' =$

[a]  $-\frac{4}{4+9x^2}$        [b]  $\frac{6}{4+9x^2}$        [c]  $-\frac{6}{4+9x^2}$        [d]  $\frac{4}{4+9x^2}$

32) The critical numbers of the function  $f(x) = 2x^3 - 3x^2 - 12x + 16$  are

[a] 1, -2       [b] -1, 2       [c] 1, 2       [d] -1, -2

33) The function  $f(x) = 2x^3 - 3x^2 - 12x + 16$  is increasing on

[a]  $(-\infty, -2) \cup (-1, \infty)$        [b]  $(-\infty, -2) \cup (1, \infty)$        [c]  $(-\infty, -1) \cup (2, \infty)$        [d]  $(-\infty, 1) \cup (2, \infty)$

34) The function  $f(x) = 2x^3 - 3x^2 - 12x + 16$  is decreasing on

[a]  $(-2, -1)$        [b]  $(-2, 1)$        [c]  $(1, 2)$        [d]  $(-1, 2)$

35) The function  $f(x) = 2x^3 - 3x^2 - 12x + 16$  has a relative maximum at

[a] (1, 3)       [b] (-1, -23)       [c] (2, -4)       [d] (-2, 12)

36) The function  $f(x) = 2x^3 - 3x^2 - 12x + 16$  has a relative minimum at

[a] (1, 3)       [b] (-1, -23)       [c] (2, -4)       [d] (-2, 12)

37) The graph of  $f(x) = 2x^3 - 3x^2 - 12x + 16$  concave upward on

[a]  $(-\infty, \frac{1}{2})$        [b]  $(-\infty, -\frac{1}{2})$        [c]  $(-\frac{1}{2}, \infty)$        [d]  $(\frac{1}{2}, \infty)$

38) The graph of  $f(x) = 2x^3 - 3x^2 - 12x + 16$  concave downward on

[a]  $(-\infty, \frac{1}{2})$        [b]  $(-\infty, -\frac{1}{2})$        [c]  $(-\frac{1}{2}, \infty)$        [d]  $(\frac{1}{2}, \infty)$

39) The function  $f(x) = 2x^3 - 3x^2 - 12x + 16$  has an inflection at

[a]  $(\frac{1}{2}, 21)$        [b]  $(-\frac{1}{2}, 21)$        [c]  $(\frac{1}{2}, \frac{19}{2})$        [d]  $(-\frac{1}{2}, \frac{19}{2})$

40) If  $y = \log_5(x^3 - 2\csc x)$ , then  $y' =$

[a]  $\frac{3x^2 + 2\csc x \cot x}{x^3 - 2\csc x \ln 5}$        [b]  $\frac{3x^2 + 2\csc x \cot x}{(x^3 - 2\csc x) \ln 5}$

[c]  $\frac{3x^2 + 2\csc x \cot x}{x^3 - 2\csc x}$        [d]  $\frac{3x^2 - 2\csc x \cot x}{(x^3 - 2\csc x) \ln 5}$

King Abdul Aziz University Faculty of Sciences Mathematics Department  
 Math 110 Final Test Fall 2013 (40 Marks) Time 120 m  
 Student Name: Student Number: D

1) If  $y = -\ln(\sin x)$ , then  $y' =$

- a*  $\tan x$     *b*  $-\tan x$     *c*  $\cot x$     *d*  $-\cot x$

2) If  $y = x^x$ , then  $y' =$

- a*  $1 + \ln x$     *b*  $x^x$     *c*  $x^x \ln x$     *d*  $x^x(1 + \ln x)$

3) If  $y = \cot^{-1}\left(\frac{3x}{2}\right)$ , then  $y' =$

- a*  $-\frac{4}{4+9x^2}$     *b*  $\frac{6}{4+9x^2}$     *c*  $-\frac{6}{4+9x^2}$     *d*  $\frac{4}{4+9x^2}$

4) If  $y = \sin^4(3x)$ , then  $y' =$

- a*  $4\sin^3(3x)\cos(3x)$     *b*  $12\sin^3(3x)\cos(3x)$   
*c*  $3\cos^2(3x)$     *d*  $3\sin^4(3x) + 12\sin^3x\cos x$

5) The tangent line equation to the curve  $y = \frac{2x}{x-1}$  at the point  $(0,0)$  is

- a*  $y = -2x - 1$     *b*  $y = -2x$   
*c*  $y = 2x$     *d*  $y = 2x + 1$

6) If  $y^2 - 2 = 3xy - x^2$ , then  $y' =$

- a*  $\frac{2x}{3-2y}$     *b*  $\frac{2x}{y}$     *c*  $\frac{3y-2x}{2y-3x}$     *d*  $\frac{2x+y}{3x-2y}$

7) If  $y = 3^x \tan x$ , then  $y' =$

- a*  $3^x \ln 3 \tan x - 3^x \sec^2 x$     *b*  $3^x \tan x - 3^x \sec^2 x$   
*c*  $3^x \ln 3 \tan x + 3^x \sec^2 x$     *d*  $3^x \tan x + 3^x \sec^2 x$

8) If  $y = (2x^2 + \csc x)^7$ , then  $y' =$

- a*  $28x(2x^2 + \csc x)^6$     *b*  $7(2x^2 + \csc x)^6$   
*c*  $7(2x^2 + \csc x)^6(4x + \csc x \cot x)$     *d*  $7(2x^2 + \csc x)^6(4x - \csc x \cot x)$

9) The slope of the perpendicular line to the line  $2y - 3x - 6 = 0$  is

- a*  $\frac{2}{3}$     *b*  $-\frac{2}{3}$     *c*  $-\frac{3}{2}$     *d*  $\frac{3}{2}$

10)  $D^{(128)}(\cos x) =$

- a)  $\sin x$        b)  $-\sin x$        c)  $\cos x$        d)  $-\cos x$

11) If  $y = \sqrt{3x^2 - 6x}$ , then  $y' =$

- a)  $\frac{6(x-1)}{\sqrt{3x^2-6x}}$        b)  $\frac{x-6}{\sqrt{3x^2-6x}}$        c)  $\frac{3(x-1)}{\sqrt{3x^2-6x}}$        d)  $\frac{x-1}{2\sqrt{3x^2-6x}}$

12) If  $y = \ln \frac{x+1}{x-2}$ , then  $y' =$

- a)  $\frac{1}{(x+1)(x-2)}$        b)  $-\frac{1}{(x+1)(x-2)}$        c)  $\frac{3}{(x+1)(x-2)}$        d)  $-\frac{3}{(x+1)(x-2)}$

13)  $\lim_{x \rightarrow 3^-} \frac{x+1}{x-3} =$

- a)  $-\infty$        b)  $-3$        c)  $\infty$        d)  $3$

14) If the graph of the function  $f(x) = 3^x$  is shifted a distance 2 units to the left, then the new graph represented the graph of the function

- a)  $3^{x+2}$        b)  $3^x + 2$        c)  $3^{x-2}$        d)  $3^x - 2$

15) If  $f(x) = x^2$ , then  $f'(x) =$

a)  $\lim_{x \rightarrow 0} \frac{(x+h)^2 + x^2}{h}$        b)  $\lim_{h \rightarrow 0} \frac{(x+h)^2 + x^2}{h}$

c)  $\lim_{h \rightarrow 0} \frac{(x+h)^2 - x^2}{h}$        d)  $\lim_{x \rightarrow 0} \frac{(x+h)^2 - x^2}{h}$

16) If  $y = \log_5(x^3 - 2\csc x)$ , then  $y' =$

a)  $\frac{3x^2 + 2\csc x \cot x}{x^3 - 2\csc x \ln 5}$        b)  $\frac{3x^2 - 2\csc x \cot x}{(x^3 - 2\csc x) \ln 5}$

c)  $\frac{3x^2 + 2\csc x \cot x}{x^3 - 2\csc x}$        d)  $\frac{3x^2 + 2\csc x \cot x}{(x^3 - 2\csc x) \ln 5}$

17)  $\lim_{x \rightarrow 0} \frac{\tan 3x}{5x} =$

- a)  $\frac{1}{5}$        b)  $\frac{5}{3}$        c)  $\frac{3}{5}$        d)  $3$

18)  $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2} =$

- a)  $\infty$        b) 0       c) 4       d)  $\frac{1}{4}$

19) The distance between the points  $(-1, 2)$  and  $(2, -1)$  is

- a) 3       b)  $2\sqrt{3}$        c)  $3\sqrt{2}$        d) 9

20)  $\frac{3\pi}{2}$  rad =

- a)  $120^\circ$        b)  $150^\circ$        c)  $270^\circ$        d)  $210^\circ$

21) The absolute minimum value of  $f(x) = x^3 - 6x^2 + 9x + 2$  on  $[0, 4]$  is

- a) 6       b) 0       c) -3       d) 2

22) The absolute maximum value of  $f(x) = x^3 - 6x^2 + 9x + 2$  on  $[0, 4]$  is

- a) 7       b) 2       c) 6       d) 12

23) The values in  $(-1, 3)$  which makes  $f(x) = x^2 - 5x + 7$  satisfied Mean Value Theorem on  $[-1, 3]$  is

- a) -4       b) 0       c) 2       d) 1

24) The domain of  $\frac{x+3}{\sqrt{4-x^2}}$  is

- a)  $(-2, 2)$        b)  $(-\infty, -2) \cup (2, \infty)$        c)  $[-2, 2]$        d)  $(-\infty, -2] \cup [2, \infty)$

25) The function  $f(x) = \frac{x+1}{x^2 - 25}$  is continuous on

- a)  $[-5, 5]$        b)  $\{x \in \mathbb{R} : x \neq \pm 5\}$        c)  $(-\infty, -5) \cup (5, \infty)$        d)  $\{\pm 5\}$

26) If  $f(x) = \cot^{-1}(x)$  and  $g(x) = \cot(x)$  then  $(f \circ g)(x) =$

- a) 1       b)  $\cot x \cot^{-1} x$        c)  $\cot x$        d)  $x$

27) If  $y = e^{2x}$ , then  $y^{(7)} =$

- a)  $128e^{2x}$        b)  $16e^{2x}$        c)  $64e^{2x}$        d)  $32e^{2x}$

28) If  $-7 < 2x + 3 < 5$ , then  $x =$

- a)  $(-5, 1)$        b)  $(-5, 1]$        c)  $[-5, 1)$        d)  $[-5, 1]$

29) If  $y = \cos x \csc x$ , then  $y' =$

- a)  $-1 + \cos x \cot x$        b)  $1 - \cos x \cot x$        c)  $-\csc^2 x$        d)  $1 - \cos x \csc x \cot x$

30)	The critical numbers of the function $f(x) = 2x^3 + 3x^2 - 12x + 16$ are						
<input type="checkbox"/> a	1, -2	<input type="checkbox"/> b	-1, 2	<input type="checkbox"/> c	1, 2	<input type="checkbox"/> d	-1, -2
31)	The function $f(x) = 2x^3 + 3x^2 - 12x + 16$ is increasing on						
<input type="checkbox"/> a	$(-\infty, -2) \cup (-1, \infty)$	<input type="checkbox"/> b	$(-\infty, -2) \cup (1, \infty)$	<input type="checkbox"/> c	$(-\infty, -1) \cup (2, \infty)$	<input type="checkbox"/> d	$(-\infty, 1) \cup (2, \infty)$
32)	The function $f(x) = 2x^3 + 3x^2 - 12x + 16$ is decreasing on						
<input type="checkbox"/> a	$(-\infty, -1) \cup (2, \infty)$	<input type="checkbox"/> b	$(-\infty, -2) \cup (1, \infty)$	<input type="checkbox"/> c	(-2, 1)	<input type="checkbox"/> d	(-1, 2)
33)	The function $f(x) = 2x^3 - 3x^2 - 12x + 15$ has a relative maximum at						
<input type="checkbox"/> a	(1, 9)	<input type="checkbox"/> b	(-1, 29)	<input type="checkbox"/> c	(2, 20)	<input type="checkbox"/> d	(-2, 36)
34)	The function $f(x) = 2x^3 + 3x^2 - 12x + 16$ has a relative minimum at						
<input type="checkbox"/> a	(1, 9)	<input type="checkbox"/> b	(-1, 29)	<input type="checkbox"/> c	(2, 20)	<input type="checkbox"/> d	(-2, 36)
35)	The graph of $f(x) = 2x^3 + 3x^2 - 12x + 16$ concave upward on						
<input type="checkbox"/> a	$(-\infty, \frac{1}{2})$	<input type="checkbox"/> b	$(-\infty, -\frac{1}{2})$	<input type="checkbox"/> c	$(-\frac{1}{2}, \infty)$	<input type="checkbox"/> d	$(\frac{1}{2}, \infty)$
36)	The graph of $f(x) = 2x^3 - 3x^2 - 12x + 15$ concave downward on						
<input type="checkbox"/> a	$(-\infty, \frac{1}{2})$	<input type="checkbox"/> b	$(-\infty, -\frac{1}{2})$	<input type="checkbox"/> c	$(-\frac{1}{2}, \infty)$	<input type="checkbox"/> d	$(\frac{1}{2}, \infty)$
37)	The function $f(x) = 2x^3 + 3x^2 - 12x + 16$ has an inflection at						
<input type="checkbox"/> a	$(\frac{1}{2}, 11)$	<input type="checkbox"/> b	$(-\frac{1}{2}, 11)$	<input type="checkbox"/> c	$(\frac{1}{2}, \frac{45}{2})$	<input type="checkbox"/> d	$(-\frac{1}{2}, \frac{45}{2})$
38)	$\lim_{x \rightarrow \infty} \left( \sqrt{x^2 + x} - x \right) =$						
<input type="checkbox"/> a	$\frac{1}{2}$	<input type="checkbox"/> b	1	<input type="checkbox"/> c	0	<input type="checkbox"/> d	$-\frac{1}{2}$
39)	$\sin(\tan^{-1} x) =$						
<input type="checkbox"/> A	$\frac{1}{\sqrt{x^2 + 1}}$	<input type="checkbox"/> B	$\frac{x}{\sqrt{x^2 + 1}}$	<input type="checkbox"/> C	$\sqrt{x^2 + 1}$	<input type="checkbox"/> D	$\frac{\sqrt{x^2 + 1}}{x}$
40)	If $f(x) = 2x + 11$ , then $f^{-1}(x) =$						
<input type="checkbox"/> a	$\frac{x + 11}{2}$	<input type="checkbox"/> b	$\frac{x - 11}{2}$	<input type="checkbox"/> c	$\frac{x}{2} + 11$	<input type="checkbox"/> d	$\frac{x}{2} - 11$